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Total No. of Pages : 02

Total No. of Questions : 09

B.Tech. (2011 to 2017) (Sem.-1)
ENGINEERING MATHEMATICS – I
Subject Code : BTAM-101
Paper ID : [A1101]

Time : 3 Hrs.

Max. Marks : 60

INSTRUCTIONS TO CANDIDATES :

1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
2. SECTION - B & C. have FOUR questions each.
3. Attempt any FIVE questions from SECTION B & C carrying EIGHT marks each.
4. Select atleast TWO questions from SECTION - B & C.
5. Symbols used have their usual meanings. Statistical tables, if demanded, may be provided.

SECTION-A

- Q1 a) Find the curvature at any point of the curve $y^2 = x^3 + 8$ at (1,3)
- b) Find the radius of curvature at any point (r, θ) of polar curve $r = a(1 + \cos\theta)$.
- c) Write down the formula for finding the volume of solid by revolving the area bounded by the curve $y=f(x)$ and the line $x=a$, $x=b$ and $y=p$ about the line $y=p$.
- d) Find the area of ellipse $\frac{x^2}{4} + \frac{y^2}{9} = 1$. <http://www.punjabpapers.com>
- e) Show that $\lim_{(x,y) \rightarrow (0,0)} \frac{x^2 + y^2}{y^2 - x^2}$ does not exist.
- f) Find $\frac{\partial w}{\partial r}$ if $w = x + 2y + z^2$, $x = \frac{r}{s}$, $y = 2r + s^2$, $z = 2r$.
- g) Write down the equation of hyperboloid of two sheet and draw its rough sketch.
- h) A particle moves along the curve $x = t^3 + 1$, $y = t^2$, $z = 2t + 5$, where t is the time variable. Find the velocity at time $t=1$.
- i) Determine whether $\vec{A} = 2xyz^3\hat{i} + x^2z^3\hat{j} + 3x^2yz^2\hat{k}$ is irrotational or not?
- j) State Stoke's theorem.

SECTION-B

- Q2 a) Sketch the curve by considering all the salient features $y = x + \frac{1}{x}$.
- b) Trace the polar curve : $r = a(1 + \sin\theta)$, $a > 0$.
- Q3 a) Find the perimeter of the circle $x^2 + y^2 = 9$.
- b) Find the surface of the solid generated by the revolution of Lemniscate $r^2 = a^2 \cos 2\theta$ about initial line.
- Q4 a) If $u = \tan^{-1} \left(\frac{x^3 + y^3}{x - y} \right)$ prove that $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial y \partial x} + y^2 \frac{\partial^2 u}{\partial y^2} = 2 \cos 3u \sin u$.
- b) If $u = f(y - z, z - x, x - y)$, then prove that $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = 0$.
- Q5 a) Expand $e^y \log(1 + y)$ in powers of x and y upto third degree.
- b) Find all the local maxima and minima of the function :

$$f(x, y) = x^3 + y^3 - 63(x + y) + 12xy$$

SECTION-C

- Q6 a) Evaluate $\iint (x^2 + y^2) dx dy$ over the circle $x^2 + y^2 = a^2$ by changing into polar coordinates. <http://www.punjabpapers.com>
- b) Evaluate the volume of the sphere $x^2 + y^2 + z^2 = 1$ by using triple integration.
- Q7 a) If \vec{A} is vector function and Φ is a scalar function then prove that :
- $$\nabla \times (\phi \vec{A}) = \phi (\nabla \times \vec{A}) + (\nabla \phi) \times \vec{A}$$
- b) if $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$, prove that $\nabla \cdot (r^n \vec{r}) = (n + 3)r^n$, where $r = |\vec{r}|$.
- Q8. Evaluate $\iint_S \vec{A} \cdot \hat{n} ds$ where $\vec{A} = 12x^2 y \hat{i} - 3yz \hat{j} + 2z \hat{k}$ and S is the portion of the plane $x + y + z = 1$ included in the first quadrant.
- Q9. Verify Green's theorem for $\oint_c (xy + y^2) dx + x^2 dy$, where c is the boundary of the closed region bounded by $y = x^2$ and $y = x$.