

Roll No.

Total No. of Pages : 03

Total No. of Questions : 09

B.Tech.(ANE) (Sem.-7,8)

THEORY OF ELASTICITY

Subject Code : ANE-414

M.Code : 70496

Time : 3 Hrs.

Max. Marks : 60

INSTRUCTIONS TO CANDIDATES :

1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt any FOUR questions.
3. SECTION-C contains THREE questions carrying TEN marks each and students have to attempt any TWO questions.

SECTION-A

1. Write briefly :

- a) What is stress-ellipsoid? What do its semi-axes represent?
- b) Write down the equilibrium equations for a plane stress problem and explain its various terms.
- c) A large plate contains a small circular hole at its centre. What is the maximum tangential stress around the periphery of the hole if the plate is subjected to a uniaxial tensile stress p_0 of the two ends of the plate?
- d) State saint-venant's theory of torsion.
- e) State and explain stress-optic law.
- f) Differentiate between 'Isoclinics' and 'Isochromatics'.
- g) What is the relation between maximum shearing stress and principal stresses?
- h) Sketch the six components of stress on an element at a point in a three dimensional strained body.
- i) Write down the stress-strain relations in polar coordinates.
- j) What do you understand by symmetrical stress distribution?

SECTION-B

2. Making suitable assumptions, derive the strain-displacement relations for a two-dimensional problem.
3. Describe the principles of photoelasticity with suitable sketches.
4. Derive the compatibility equation for a plane stress problem in the absence of body forces.
5. A bar of a narrow rectangular cross-section and with a circular axis is constrained at the lower end and bent by a force P applied at the upper end in a radial direction as shown in Fig. 1.

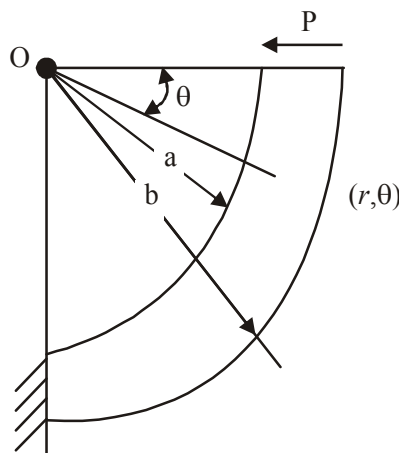


Fig.1

Assuming a stress functions :

$$\phi = \left(Ar^3 + \frac{B}{r} + Cr + Dr \log r \right) \sin \theta$$

Determine the stress components, δ_r , δ_θ and $\tau_{r\theta}$.

6. The radial stress in a rotating disc of inner radius a and outer radius b is given by :

$$\delta_r = \left(\frac{3+\nu}{8} \right) \rho \omega^2 \left[b^2 + a^2 - \frac{a^2 b^2}{r^2} - r^2 \right]$$

Where ω = Angular velocity of the disc

ν = Poisson's ratio

ρ = Density of disc material

Determine the maximum value of δ_r .

SECTION-C

7. A prismatical bar is bent in one of its principal planes by two equal and opposite couples M . Making suitable assumptions, derive expressions for the displacements u , v and w .
8. A cantilever of length L and depth $2h$ is in a state of plane stress. The cantilever is unit of thickness, is rigidly supported at the end $x = L$ and is loaded as shown in Fig. 2.

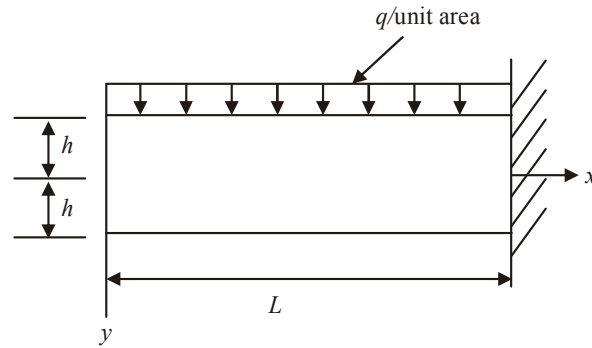


Fig.2

Show that the stress function :

$$\phi = Ax^2 + Bx^2y + cy^3 + D(5x^2y^3 - y^5)$$

is valid for the beam and evaluate constants A , B , C and D .

9. Show that the warping function

$\psi = kxy$, in which k is an unknown constant, may be used to solve the torsion problem for the elliptical section.

NOTE : Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.