Roll No.

Total No. of Pages: 02

Total No. of Questions: 09

B.Tech.(ME) (2012 Onwards) (Sem.-5)

**MATHEMATICS-III** 

Subject Code: BTAM-500

M.Code: 70601

Time: 3 Hrs. Max. Marks: 60

#### **INSTRUCTION TO CANDIDATES:**

- SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
- 2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt ANY FOUR questions.
- SECTION-C contains THREE questions carrying TEN marks each and students have to attempt ANY TWO questions.

### **SECTION-A**

# 1. Write briefly:

- a) Expand  $f(z) = \frac{z}{(z+1)(z+2)}$  about z = -2.
- b) Evaluate  $\int_C \frac{\sin z}{z \cos z} dz$  along the circle C : |z| = 2.
- c) Find the bilinear transformation that map the points z = 1, -i 1 into the points w = i, 0, -i.
- d) Find L  $(t^2 \sin 3t)$ .
- e) Form a partial differential equation from z = f(x + 4t) + g(x 4t).
- f) Find the solution of homogeneous partial differential equation 2r 5s + 2t = 0.
- g) Write Dirichlet's conditions for the expansion of f(x) as a Fourier series in the interval  $(-\pi, \pi)$ .
- h) Show that  $P_n(-x) = (-1)^n P_n(x)$ .
- i) State Cauchy's Residue theorem.
- j) Find the coefficient  $a_0$  in the Fourier series of  $f(x) = |x|, -\pi \le x \le \pi$ .

## **SECTION-B**

2. Prove that 
$$\int J_3(x) dx = -J_2(x) - \frac{2}{x} J_2(x)$$
.

- 3. Expand  $f(x) = x \sin x$ ,  $-\pi \le x \le \pi$  as a Fourier series.
- 4. State convolution theorem and hence evaluate  $L^{-1}\left[\frac{s^2}{(s^2+4)(s^2+9)}\right]$ .
- 5. If f(z) = u + iv is an analytic function, then find f(z) if  $u + v = \frac{x}{x^2 + v^2}$ .
- 6. Solve the following partial differential equation by method of separation of variables:

$$4\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} = 3u$$
, Given that  $u = 3e^{-y} - e^{-5y}$  when  $x = 0$ 

### **SECTION-C**

- 7. Use the concept of residues to evaluate  $\int_0^{\pi} \frac{d\theta}{(a+b\cos\theta)}$ , where a > |b|.
- 8. A tightly stretched string has its ends fixed at x = 0 and x = 1. At time t = 0, the string is given a shape defined by  $f(x) = \lambda x (1 x)$ , where  $\lambda$  is constant and then released. Find the displacement of any point x of the string at any time t > 0.
- 9. Solve in series the equation :

$$(1+x^2)v''+xv'-v=0$$

NOTE: Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.