Roll No.

Total No. of Pages: 02

Total No. of Questions: 11

M.Sc. (Mathematics) (2018 Batch) (Sem.-3)

MATHEMATICAL STATISTICS

Subject Code: MSM-303-18 M.Code: 76674

Time: 3 Hrs. Max. Marks: 70

INSTRUCTIONS TO CANDIDATES:

- SECTION-A is COMPULSORY consisting of FIVE questions carrying TWO marks each.
- 2. SECTION B & C. have THREE questions each.
- 3. Attempt any FOUR questions from SECTION B & C carrying FIFTEEN marks each.
- 4. Select atleast TWO questions from SECTION B & C each.

SECTION-A

- 1. Explain the term "lack of memory".
- 2. What *t*-distribution approaches normal distribution?
- 3. Define the term level of significance.
- 4. If A and B are events such that $P(A) \neq 0$, $P(B) \neq 0$ and A is independent of B, then prove that B is independent of A.
- 5. State Markov's Theorem.

SECTION-B

- 6. a) A random variable X is distributed at random between the values 0 and 1 so that its probability density function is $f(x) = kx^2 (1 x^3)$ where k is constant. Find the value of k. Using this value of k, find its mean and variance.
 - b) $X_1, X_2, ..., X_n$ be a sequence of mutually independent random variables with common distribution suppose X_k assumes only positive integral values and $E(X_k)=0$ exist; k=1, 2, ..., n and $S_n=X_1+X_2+...+X_n$ then show that

$$E\left(\frac{S_m}{S_n}\right) = \frac{m}{n}$$

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7. a) X_1 and X_2 are independent random variables, then prove that

$$\phi_{X_1+X_2}(t) = \phi_{X_1}(t) \phi_{X_2}(t)$$

b) Find the moment generating function of the random variable whose moments are

$$\mu_r' = (r+1)! 2^r$$

- 8. a) State and prove multiplicative theorem of probability for independent events.
 - b) Two computers A and B are to be marketed. A salesman who is assigned the job of finding customers for them has 60% and 40% chances respectively of succeeding in case of computers A and B. The two computers can be sold independently. Given that he was also able to sell at least one computer, what is the probability that computer A has been sold?

SECTION-C

- 9. Define binomial distribution. Obtain mean deviation about mean of binomial distribution and mode of binomial distribution.
- 10. Explain how you will use hyper geometric model to estimate the number of fish in a lake.
- 11. a) Define chi-square distribution. Obtain its M.G.F.
 - b) Prove that a linear combination of independent normal variates is also a normal variate.

NOTE: Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.

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