Roll No.

Total No. of Pages: 02

Total No. of Questions: 07

M.Sc. Mathematics (2017 Batch) (Sem.-2)

**ALGEBRA-II** 

Subject Code: MSM-201 Paper ID: [75008]

Time: 3 Hrs. Max. Marks: 80

#### **INSTRUCTIONS TO CANDIDATES:**

- SECTION-A is COMPULSORY consisting of EIGHT questions carrying TWO marks each.
- SECTION B & C. have THREE questions in each section carrying SIXTEEN marks each.
- 3. Select atleast TWO questions from SECTION B & C EACH.

### **SECTION-A**

# Q1. Answer briefly:

- a) Define UFD.
- b) Prove that every field is principal ideal domain.
- c) Use Eisenstein's criterion to prove that the following polynomials are irreducible over Q.
  - i)  $x^2+1$
  - ii)  $x^2-3x+4$
- d) State Gauss lemma.
- e) Show that no finite field is algebraically closed.
- f) State Fundamental theorem of Algebra.
- g) Discuss PID.
- h) Find splitting fields of the polynomial  $x^4+x^2+1$ .

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## **SECTION-B**

- Q2. Prove that Every Euclidean Domain is P.I.D.
- Q3. State and prove Eisenstein's Criterion.
- Q4. Prove that any finite extension of a finite field is a Galois extension.

## **SECTION-C**

- Q5. State and prove fundamental theorem of Galois Theory.
- Q6. Prove that every finite separable extension is a simple extension.
- Q7. Prove that a field is finite if and only if its multiplicative group is cyclic.

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