

Total No. of Pages: 02

Total No. of Questions: 07

M.Sc Mathematics (2017 Batch) (Sem.-2) PARTIAL DIFFERENTIAL EQUATIONS

Subject Code: MSM-204 M.Code: 75011

Time: 3 Hrs. Max. Marks: 80

INSTRUCTION TO CANDIDATES:

- SECTION-A is COMPULSORY consisting of EIGHT questions carrying TWO marks each.
- 2. SECTION B & C. have THREE questions in each section carrying SIXTEEN marks each.
- 3. Select atleast TWO questions from SECTION B & C each.

SECTION-A

1. Answer the following:

- a) Form the partial differential equation by eliminating the arbitrary function from $f(x^2 + y^2, z xy) = 0$.
- b) Classify the partial differential equation $u_{xx} + u_{yy} = f(x, y)$.
- c) Find the complete solution of the partial differential equation $p^3 q^3 = 0$
- d) Write all possible solutions of two-dimensional Laplace equation.
- e) Solve $(D^3 D^2 D' 8 D D'^2 + 12D'^3)z = 0$.
- f) Give an example of a linear and nonlinear partial differential equation.
- g) Find the partial differential equation of all surfaces of revolution having z-axis as the axis of rotation.
- h) State the assumptions in deriving one-dimensional wave equation.

1 M-75011 (S30)-1753

SECTION-B

- 2. a) Find the partial differential equation of all planes which are at a constant distance *k* units from the origin. (8)
 - b) Find the equation of the system of surfaces which cut orthogonally the cones of the system $x^2 + y^2 + z^2 = cxy$. (8)
- 3. a) Show that the characteristics of the equation Rr + Ss + Tt = f(x, y, z, p, q) are invariant with respect to any transformations of the independent variables. (10)
 - b) Find the complete integral of the partial differential equation $(p^2 + q^2) x = pz$ and deduce the solution which passes through the curve x = 0, $z^2 = 4y$. (6)
- 4. a) Solve the equation r + (a + b) s + abt = xy by Monge's method. (8)

b) Solve:
$$(D^3 - 2D^2 D')z = 2e^{2x} + 3x^2y$$
. (8)

SECTION-C

- 5. a) Solve $p^2x + q^2y = z$ by Jacobi's method. (8)
 - b) Find the complete solution of $p^2 + x^2y^2q^2 = x^2z^2$. (8)
- 6. Find the solution of three dimensional diffusion equation in the region 0 < x < a, 0 < y < b, 0 < z < c, t > 0, $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} = \frac{1}{k} \frac{\partial u}{\partial t}$ with the boundary and initial conditions: u(0, y, z, t) = 0 = u(a, y, z, t); u(x, 0, z, t) = 0 = u(x, b, z, t); u(x, y, 0, t) = 0 = u(x, y, z, t) and u(x, y, z, 0) = f(x, y, z). (16)
- 7. A tightly stretched violin string of length l and fixed at both ends is plucked at x = l/3 and assumes initially the shape of a triangle of height a. Find the displacement u(x, t) at any distance x and any time t after the string is released from rest. (16)

NOTE: Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.

2 M-75011 (S30)-1753