(20)



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M.Tech (Microelectronics) (Sem.-1)

ADVANCED MATHEMATICS FOR ENGINEERS

Subject Code: ME-807 M.Code: 38407

Time: 3 Hrs. Max. Marks: 100

INSTRUCTIONS TO CANDIDATES:

- 1. Attempt any FIVE questions out of EIGHT questions.
- 2. Each question carries TWENTY marks.
- 1. a) Find the Fourier sine and cosine transforms of $f(x) = e^{-ax}$. (10)
 - b) State and prove change of scale property of Fourier transforms. (10)
- 2. (a) Find the Z-transform of $c^k \cos \alpha k, k \ge 0$. (10)

b) If
$$Z(f(k)) = F(z)$$
 then show that $Z(kf(k)) = z \frac{d}{dz} F(z)$. (10)

3. Apply Crout's method to solve the equations

$$3x + 2y + 7z = 4$$
; $2x + 3y + z = 5$; $3x + 4y + z = 7$ (20)

- 4. Find the bilinear transformation which maps the points z = 1, i, -1 into the points w = i, 0, -i. Hence, find the image of |z| < 1. (20)
- 5. Define Euler's equation and prove that the shortest distance between two points in a plane is a straight line. (20)
- 6. Define convolution of two functions f(x) and g(x). State and prove convolution theorem on Fourier transforms. (20)
- 7. Determine the largest eigen value and the corresponding eigen vector of the matrix. (20)

$$A = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$$

8. Discuss Hamilton's principle and derive Lagrange's equation.

NOTE: Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.

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